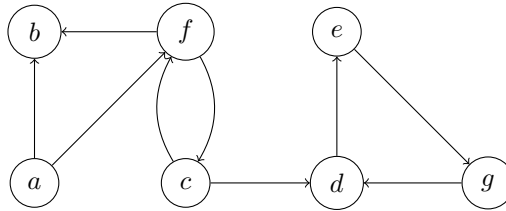

DSC 40B - Discussion 07

Problem 1.

Consider a *breadth*-first search on the graph shown in the figure, starting with node *c*.



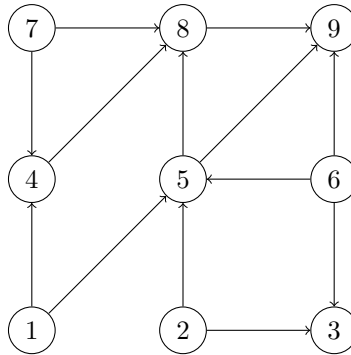
- a) Suppose you call `bfs_shortest_paths(graph, 'c')` on the graph above. This function returns dictionaries `distance` and `predecessor`. Write down the contents of these dictionaries as they are when the function exits.

```
def bfs_shortest_paths(graph, source):
    status = {node: 'undiscovered' for node in graph.nodes}
    distance = {node: float('inf') for node in graph.nodes}
    predecessor = {node: None for node in graph.nodes}
    status[source] = 'pending'
    distance[source] = 0
    pending = deque([source])
    # while there are still pending nodes
    while pending:
        u = pending.popleft()
        for v in graph.neighbors(u):
            # explore edge (u,v)
            if status[v] == 'undiscovered':
                status[v] = 'pending'
                distance[v] = distance[u] + 1
                predecessor[v] = u
                # append to right
                pending.append(v)
        status[u] = 'visited'
    return predecessor, distance
```

- b) Mark the BFS trees produced on executing BFS on this graph.

Problem 2.

Consider the following directed graph.



- a) Run Full_DFS on the graph above. Make a bold arrow from node u to node v if u is the predecessor of node v in DFS. Use the convention that a node's neighbors are processed in ascending order by label.
- b) Fill in the table below so that it contains the start and finish times of each node after a Full_DFS is performed on the above graph. Assume node 1 as the source for the first DFS call. Begin your start times with 1.

Node	Start	Finish	Node	Start	Finish
1			6		
2			7		
3			8		
4			9		
5					

Problem 3.

Given an undirected graph $G=(V,E)$, give an algorithm to find if the graph is disconnected.